

CMR TECHNICAL CAMPUS

UGC AUTONOMOUS

B. Tech. III Semester Supply End Examinations, August-2023

Statistical and Numerical Methods

Common to CE, CSE & IT

Time: 3 Hours

Max. Marks: 70

Note

- This Question paper contains Part- A and Part- B.
- All the Questions in Part A are to be answered compulsorily.
- All Questions from Part B are to be answered with internal choice among them.

PART-A

10 X 02 = 20 Marks

	Marks	CO	BL																
1. a For the following distribution find the missing probability	2M	CO1	L3																
<table border="1"> <tr> <td>X</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr> <td>P(X)</td> <td>0.001</td> <td>0.01</td> <td>0.1</td> <td>?</td> <td>0.1</td> <td>0.01</td> <td>0.001</td> </tr> </table>	X	-3	-2	-1	0	1	2	3	P(X)	0.001	0.01	0.1	?	0.1	0.01	0.001			
X	-3	-2	-1	0	1	2	3												
P(X)	0.001	0.01	0.1	?	0.1	0.01	0.001												
b List the properties of probability distribution function	2M	CO1	L1																
c Define point and interval estimations with an example for each	2M	CO2	L1																
d Define types of errors in sampling	2M	CO2	L1																
e Explain about Student's t-distribution	2M	CO3	L1																
f List the properties of chi- square test	2M	CO3	L1																
g Define root of an equation graphically	2M	CO4	L2																
h If $y = a_0 + a_1x + a_2x^2$ then give the normal equations	2M	CO4	L3																
i Using Euler's method find $y(0.1)$ if $y' = x - y^2$, $y(0) = 1$	2M	CO5	L3																
j Write the formula for trapezoidal rule	2M	CO5	L2																

PART- B

5 X 10 = 50 Marks

	Marks	CO	BL																		
2. a A random variable X has following P.D. Find (i) k (ii) $P(X>6)$ (iii) Find Mean	5M	CO1	L3																		
<table border="1"> <tr> <td>X</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>P(X)</td> <td>0</td> <td>k</td> <td>2k</td> <td>2k</td> <td>3k</td> <td>k^2</td> <td>$2k^2$</td> <td>$7k^2+k$</td> </tr> </table>	X	0	1	2	3	4	5	6	7	P(X)	0	k	2k	2k	3k	k^2	$2k^2$	$7k^2+k$			
X	0	1	2	3	4	5	6	7													
P(X)	0	k	2k	2k	3k	k^2	$2k^2$	$7k^2+k$													
b If the probability density function of a random variable X is	5M	CO1	L2																		
$f(x) = \begin{cases} \frac{1}{2} \sin x, & \text{for } 0 \leq x \leq \pi \\ 0, & \text{otherwise} \end{cases}$																					

Find the mean, median and mode

OR

3 a In tossing a coin 10 times simultaneously. Find the	5M	CO1	L2
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probability of getting

i) at least 7 heads ii) at most 3 heads iii) exactly 6 heads

- b A car hire firm has 2 cars which it hires out day by day. The number of demands for a car on each day is distributed as poisson with mean 1.5 Calculate the proportion of days
- i) on which there is no demand
- ii) on which demand is refused

5M CO1 L2

- 4 A population consists of 5, 10, 14, 18, 13, 24. Consider all possible samples of size 2 which can be drawn a) with and b) without replacement from the population. Find
- i) The mean of the population ii) Standard deviation of the population
- iii) The mean of the sampling distribution of means
- iv) Standard deviation of the sampling distribution of means

10M CO2 L5

OR

- 5 a Write the procedure for testing of hypothesis
- b A sample of the height of 6400 Englishmen has a mean of 67.85 inches and a S.D of 2.56 inches while another sample of heights of 1600 Austrians has a mean of 68.55 inches and S.D of 2.52 inches. Do the data indicate that Austrians are on the average taller than the Englishmen ? (Use α as 0.01)

5M CO2 L4

- 6 Ten specimens of copper wires drawn from a large lot have the following breaking strength (in kg) 518, 572, 570, 568, 572, 578, 572, 569, 548. Test whether the mean breaking strengths of the lot may be taken to be 518 kg weight

10M CO3 L4

OR

- 7 On the basis of information given below about the treatment of 200 patients suffering from disease, state whether the new treatment is comparatively Superior to the conventional treatment.

10M CO3 L4

Treatment	Favorable	Not Favorable	Total
New	60	30	90
Conventional	40	70	110

- 8 a Using Newton Raphson method find square root of a number

5M CO4 L2

b Find root of the equation $x^3 - 5x + 1 = 0$ using bisection method in 5 stages 5M CO4 L3

OR

9 a The temperatures T (in °C) and lengths L (in mm) of a heated rod are given below. If $L = a_0 + a_1T$, find the best values for a_0 and a_1 . 5M CO4 L3

T	20	30	40	50	60	70
L	800.3	800.4	800.6	800.7	800.9	801.0

b Fit the curve of the form $y = ae^{bx}$ to the following data 5M CO4 L3

X	77	100	185	239	285
Y	2.4	3.4	7	11.1	19.6

10 Evaluate $\int_0^1 \frac{1}{1+x} dx$ by using i) Trapezoidal rule ii) Simpson's $\frac{1}{3}$ rule iii) Simpson's $\frac{3}{8}$ rule and compare with its actual value 10M CO5 L5

OR

11 $y' = x - y^2, y(0)=1$ Using Taylor series method. And compute $y(0.1), y(0.2)$ 10M CO5 L5

CO : Course Outcomes

BL : Bloom's Taxonomy Levels

L 1 : Remembering	L 2 : Understanding
L 3 : Applying	L 4 : Analysing
L 5 : Evaluating	L 6 : Creating

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